

***The Aircraft Engine Design Project  
Fundamentals of Engine Cycles***

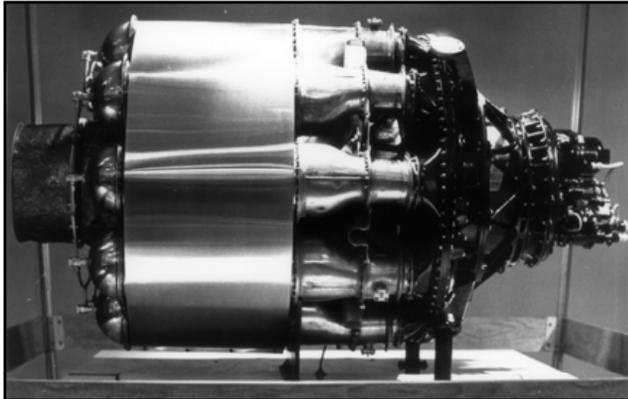


Spring 2009

Ken Gould  
Phil Weed

# g GE Aviation Technical History

GE Aircraft Engines



I-A - First U.S. jet engine  
(Developed in Lynn, MA, 1941)

U.S. jet engine

U.S. turboprop engine

Variable stator engine

Mach 2 fighter engine

Mach 3 bomber engine

High bypass engine

Variable cycle turbofan engine

Unducted fan engine

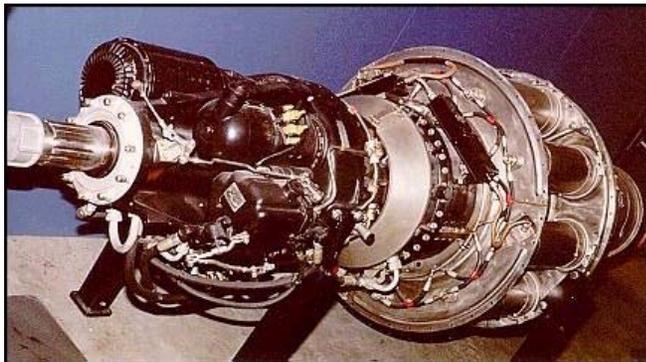
30:1 pressure ratio engine

Demonstration of 100k+ engine thrust

Certified double annular combustor engine

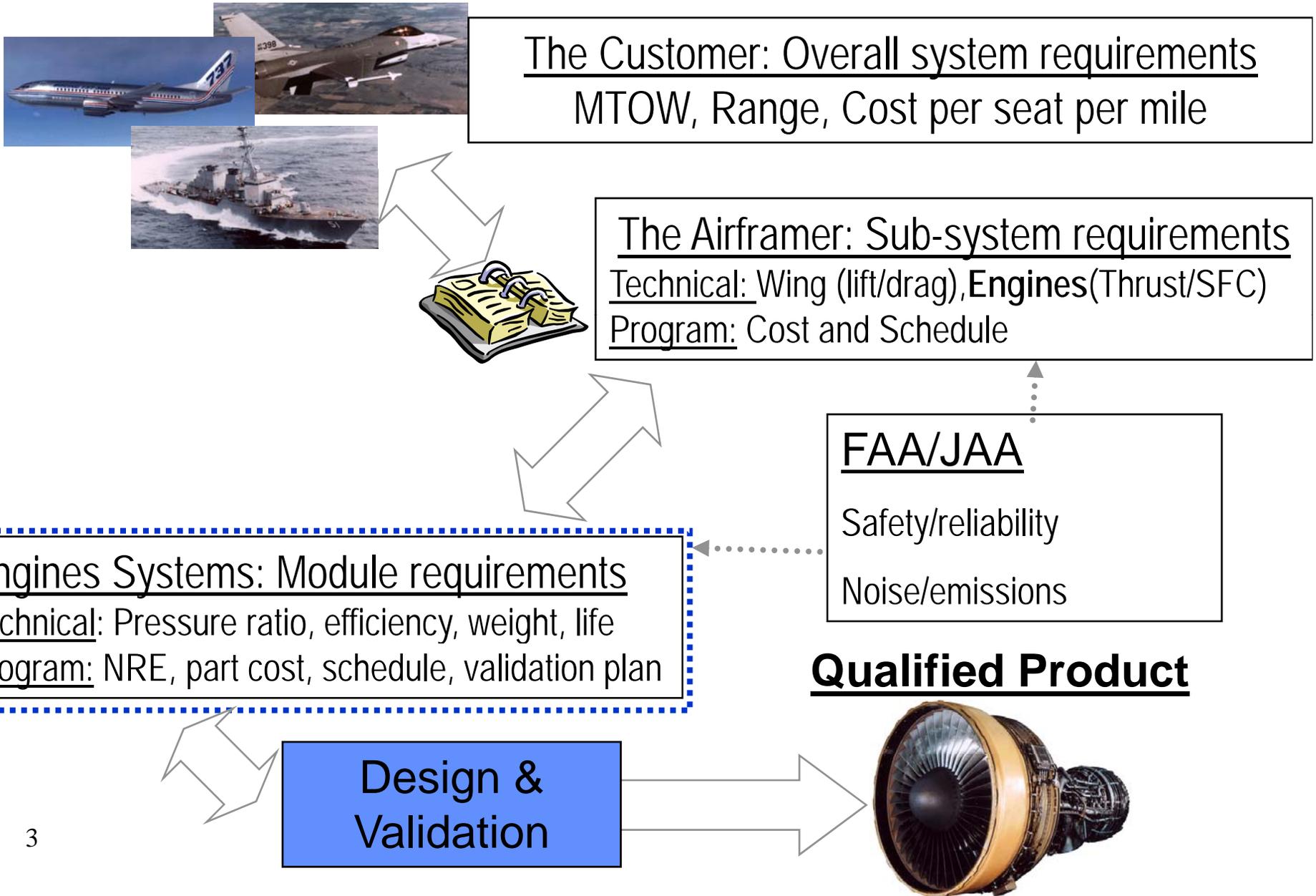


GE90 on test

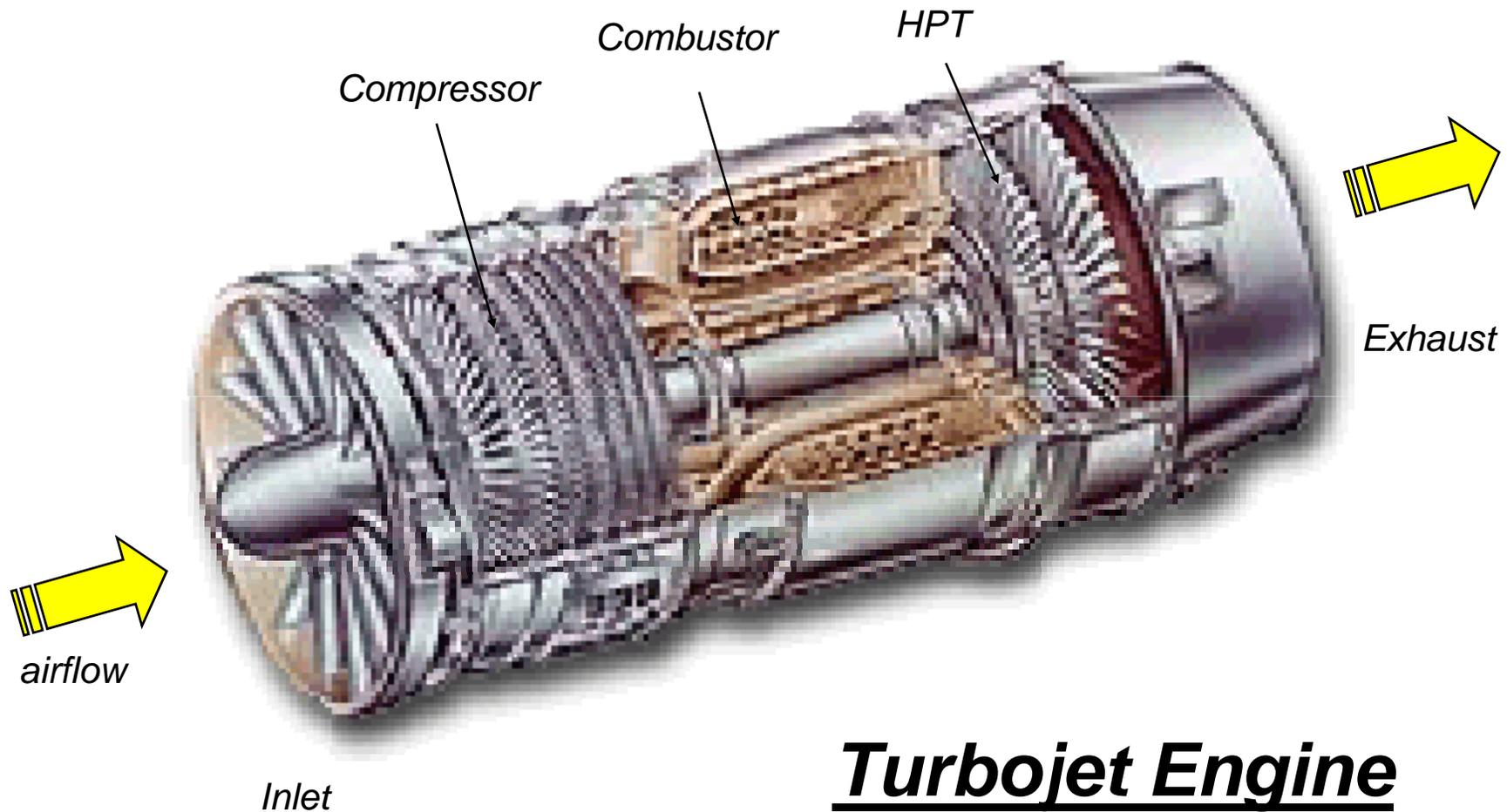


First U.S. turboprop powered aircraft, Dec. 1945

# q *Flowdown of Requirements*

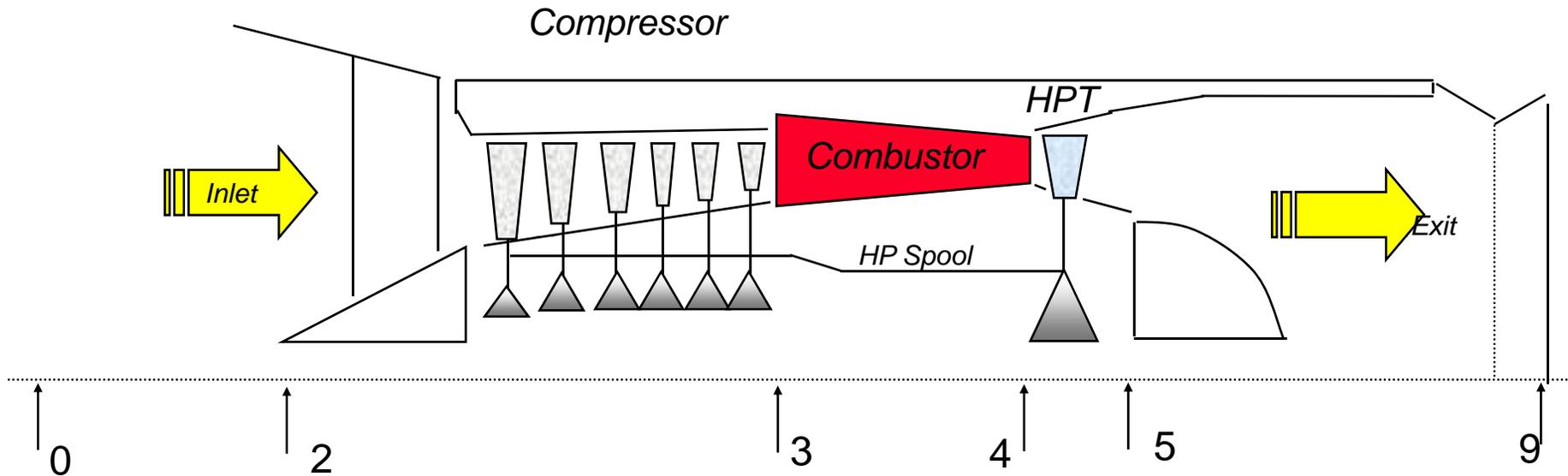


## The Aircraft Engine Design Project Fundamentals of Engine Cycles



# q Turbojet Stations

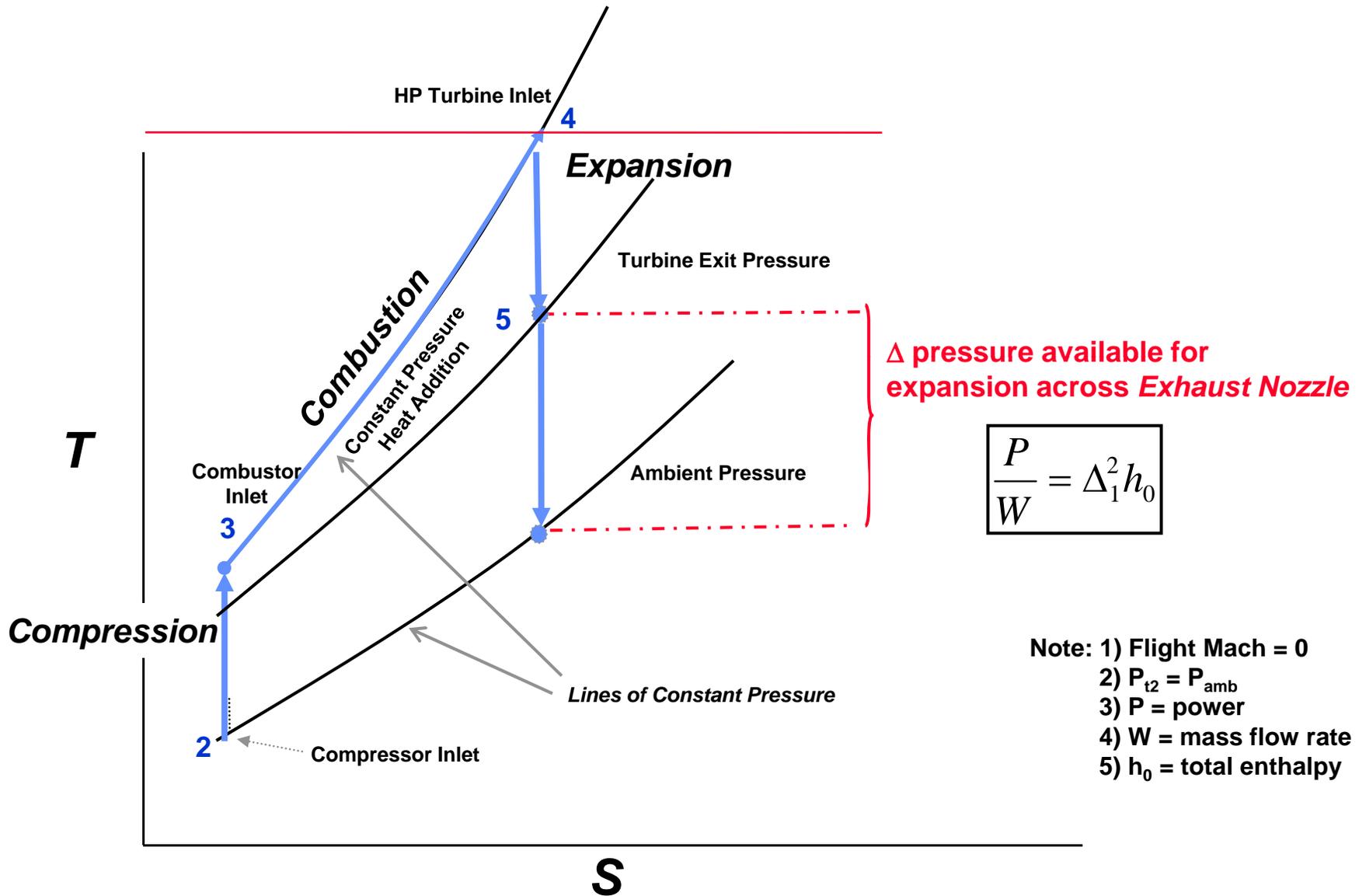
## Engine Modules and Components



## Turbojet Engine Cross-Section

*Multi-stage compressor module  
powered by a single stage turbine*

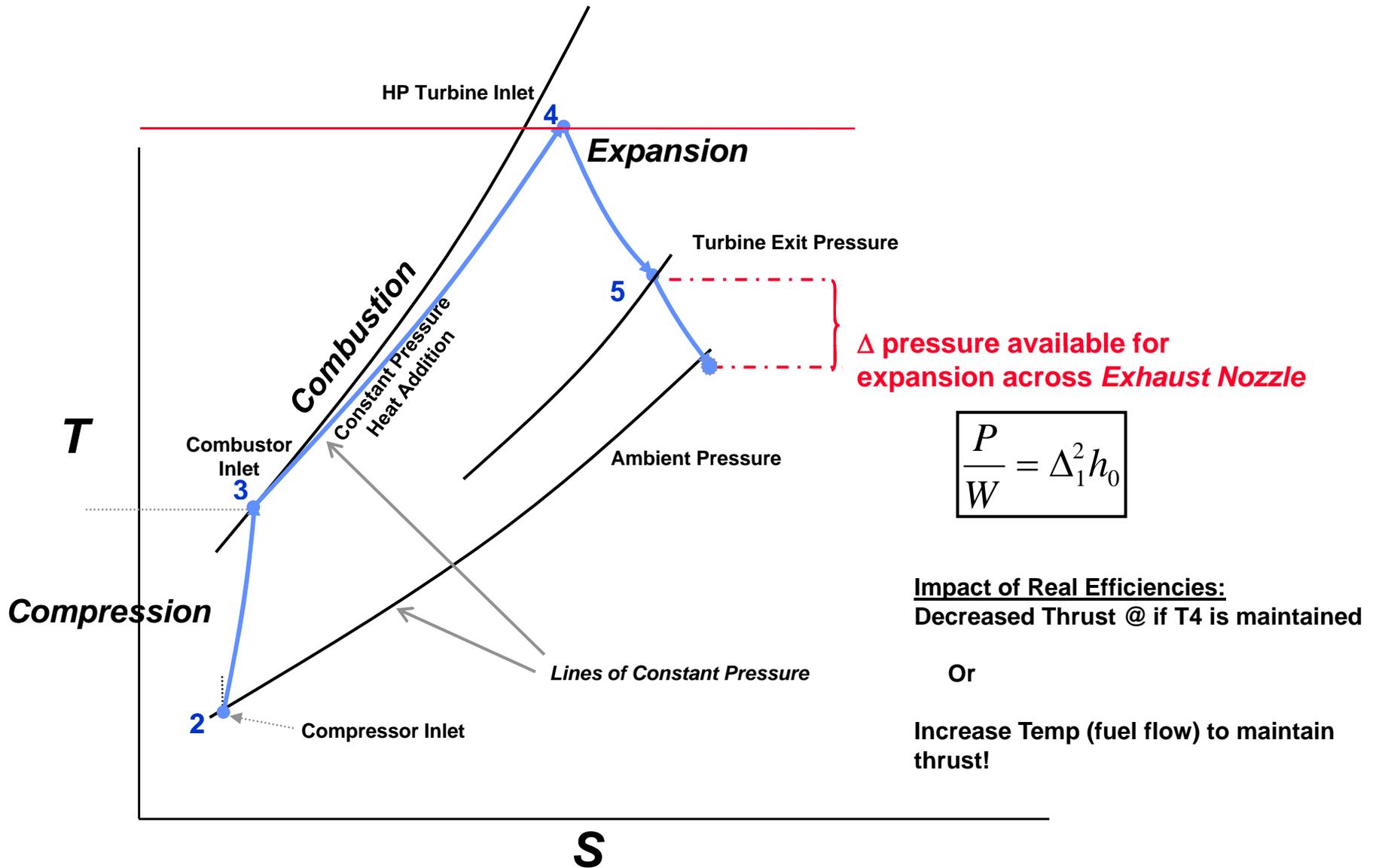
# q Ideal Brayton Cycle: T-S Representation



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# Real Brayton Cycle: T-S Representation

GE Aircraft Engines



# q Jet Engine Cycle Analysis

## Engine Inlet

- Flow capacity (flow function relationship)

Starting with the conservation of mass and substituting the total to static relations for Pressure and Temperature, can derive:

$$W = \text{Density} * \text{Area} * \text{Velocity}$$

$$\frac{W * (\text{sqrt}(T_t))}{P_t * A_e} = \frac{M * \text{sqrt}(g_c * \gamma / R)}{[1 + ((\gamma - 1) / 2) * M^2]^{(\gamma + 1) / [2 * (\gamma - 1)']}}$$

where M is Mach number

T<sub>t</sub> is total temperature (deg R)

P<sub>t</sub> is total pressure (psia)

W is airflow (lbm/sec)

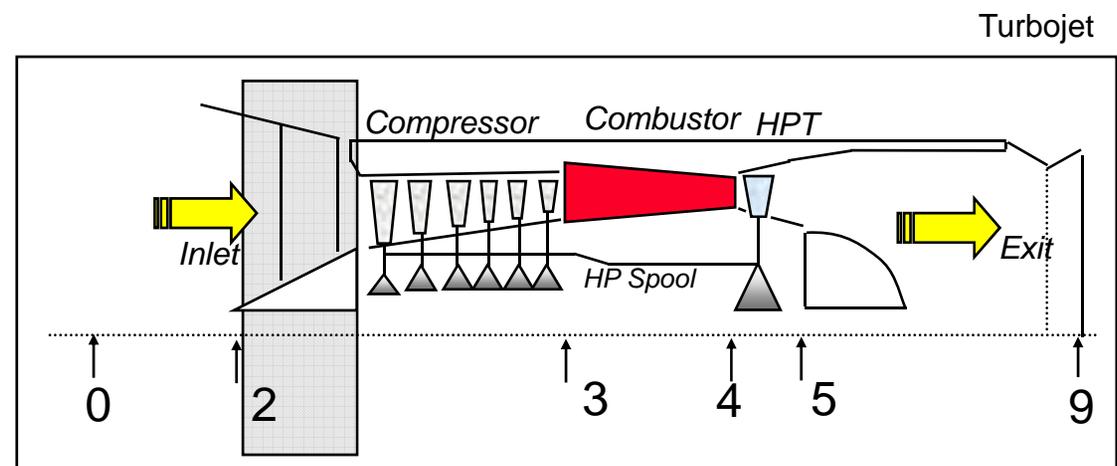
A<sub>e</sub> is effective area (in<sup>2</sup>)

g<sub>c</sub> is gravitational constant  
= 32.17 lbm ft/(sec<sup>2</sup> lbf)

γ is ratio of specific heats

R is gas constant

(ft-lbf)/(lbm-deg R)



# 9 Jet Engine Cycle Analysis

## Compressor

- From adiabatic efficiency relationship

$$\eta_{\text{compressor}} = \text{Ideal Work} / \text{Actual Work} = \frac{C_p^*(T_{\text{exit}'} - T_{\text{inlet}})}{C_p^*(T_{\text{exit}} - T_{\text{inlet}})}$$
$$= \frac{(P_{\text{exit}}/P_{\text{inlet}})^{(\gamma-1)/\gamma} - 1}{T_{\text{exit}}/T_{\text{inlet}} - 1}$$

where

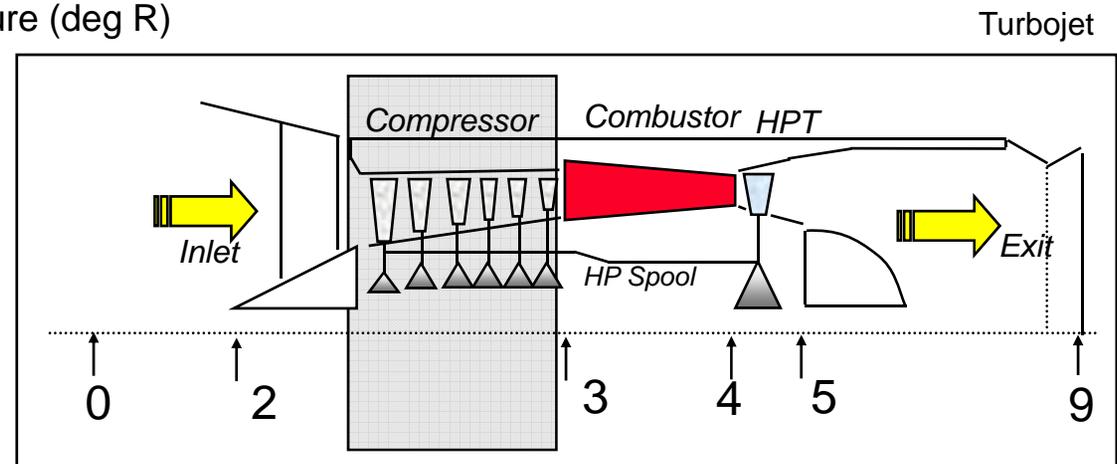
$P_{\text{exit}}$  is compressor exit total pressure (psia)

$P_{\text{inlet}}$  is compressor inlet total pressure (psia)

$T_{\text{inlet}}$  is compressor inlet total temperature (deg R)

$T_{\text{exit}}$  is compressor exit total temperature (deg R)

$T_{\text{exit}'}$  is ideal compressor exit temperature (deg R)



# q Jet Engine Cycle Analysis

## Combustor

- From Energy balance/ Combustor efficiency relationship:

$$\eta_{\text{combustor}} = \frac{\text{Actual Enthalpy Rise} / \text{Ideal Enthalpy Rise}}{\text{WF} * \text{FHV}}$$
$$= \frac{(WF + W) * C_{p_{\text{combustor}}} T_{\text{exit}} - W * C_{p_{\text{combustor}}} T_{\text{inlet}}}{\text{WF} * \text{FHV}}$$

where W is airflow (lbm/sec)

WF is fuel flow (lbm/sec)

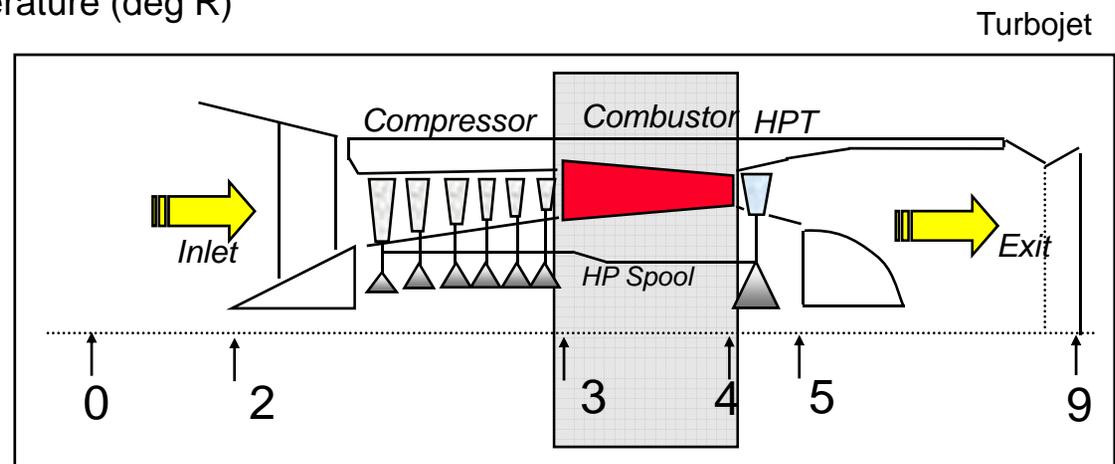
FHV is fuel heating value (BTU/lbm)

T<sub>inlet</sub> is combustor inlet total temperature (deg R)

T<sub>exit</sub> is combustor exit total temperature (deg R)

C<sub>p</sub> is combustor specific heat  
BTU/(lbm-deg R)

Can express WF/W as  
fuel to air ratio (FAR)



# q Jet Engine Cycle Analysis

## Turbine

- From efficiency relationship

$$\eta_{\text{turbine}} = \text{Actual Work/Ideal Work} = \frac{C_p^*(T_{\text{inlet}} - T_{\text{exit}})}{C_p^*(T_{\text{inlet}} - T_{\text{exit}}')}$$

$$= \frac{1 - (T_{\text{exit}}/T_{\text{inlet}})}{1 - (P_{\text{exit}}/P_{\text{inlet}})^{(\gamma-1)/\gamma}}$$

- Work Balance: From conservation of energy

Turbine Work = Compressor Work + Losses

$$(W + W_F) * C_{p_{\text{turb}}} * (T_{\text{inlet}} - T_{\text{exit}})|_{\text{turb}} = W * C_{p_{\text{compressor}}} * (T_{\text{exit}} - T_{\text{inlet}})|_{\text{comp}}$$

where

$P_{\text{exit}}$  is turbine exit total pressure (psia)

$P_{\text{inlet}}$  is turbine inlet total pressure (psia)

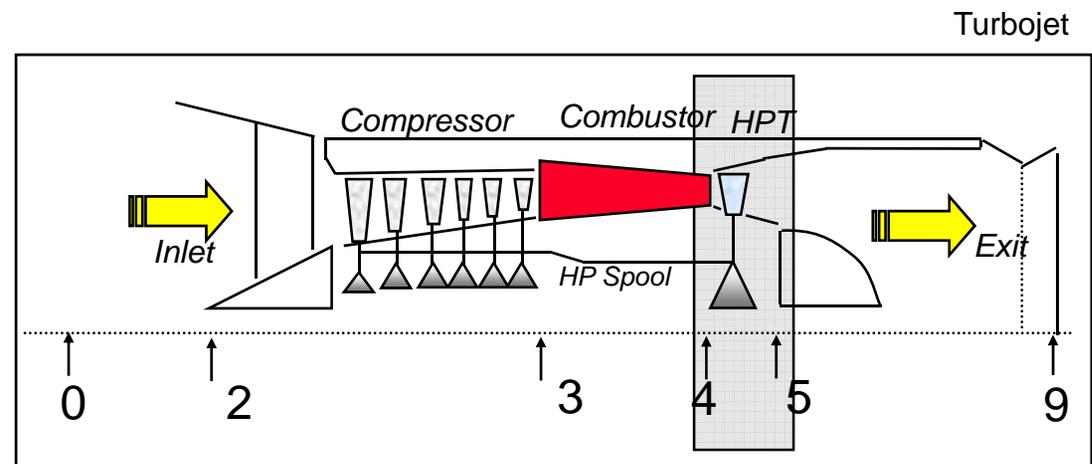
$T_{\text{inlet}}$  is inlet total temperature (deg R)

$T_{\text{exit}}$  is exit total temperature (deg R)

$T_{\text{exit}}'$  is ideal exit total temperature (deg R)

$C_p$  is specific heat for turbine or compressor

BTU/(lbm-deg R)



# q Jet Engine Cycle Analysis

## Nozzle

- Isentropic relationship, can determine exhaust properties

$$\begin{aligned} T_t/T_s &= (P_t/P_s)^{(\gamma-1)/\gamma} \\ &= 1 + ((\gamma - 1)/2) * M^2 \end{aligned}$$

- From Mach number relationship can determine exhaust velocity

$$v = M * a$$

$$\text{where } a, \text{ speed of sound} = \sqrt{\gamma * g_c * R * T_s}$$

where

$T_t$  is total temperature (deg R)

$P_t$  is total pressure (psia)

$P_s$  is static pressure (psia)

$T_s$  is static temp (deg R)

$g_c$  is gravitational constant  
= 32.17 lbf/(sec<sup>2</sup> lbf)

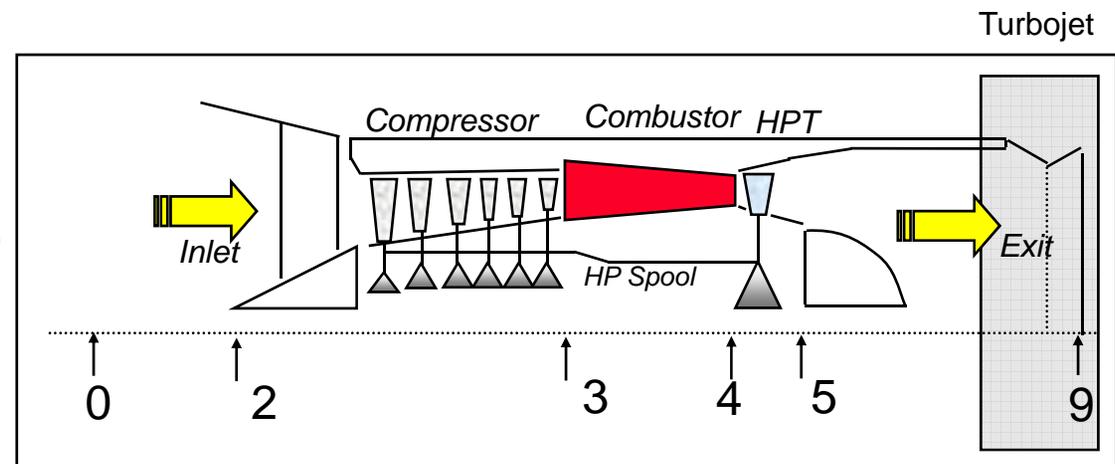
$\gamma$  is ratio of specific heats

$R$  is gas constant (ft-lbf)/(lbf-deg R)

$v$  is flow velocity (ft/sec)

$a$  is speed of sound (ft/sec)

$M$  is Mach number



# q Jet Engine Cycle Analysis

## Engine Performance

- Thrust relationship: from conservation of momentum

$$F_{net} = W_9 V_9 / g_c - W_0 V_0 / g_c + (P_{s9} - P_{s0}) A_9$$

If flight Mach number is 0,  $v_0 = 0$

and if nozzle expands to ambient,  $P_{s9} = P_{s0}$  and

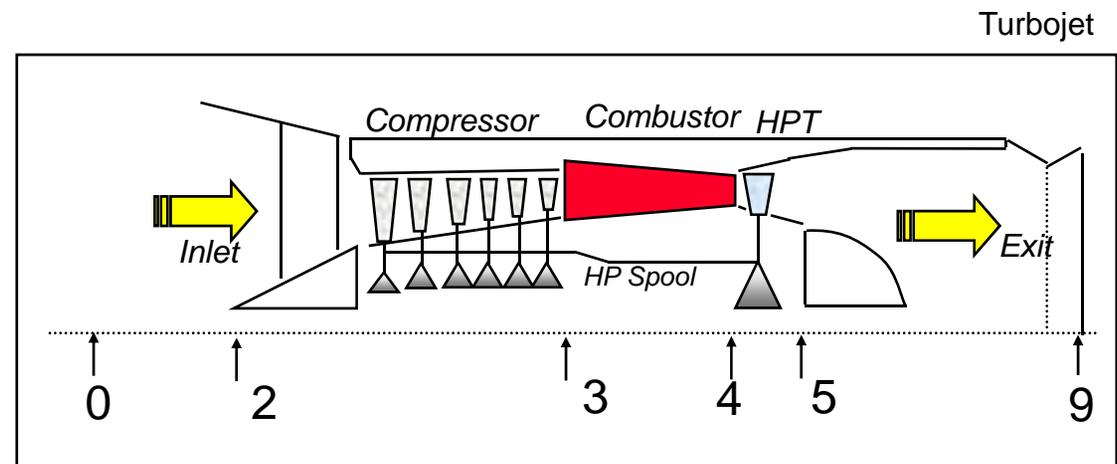
$$F_{net} = W_9 V_9 / g_c$$

where  $g_c$  is gravitational constant

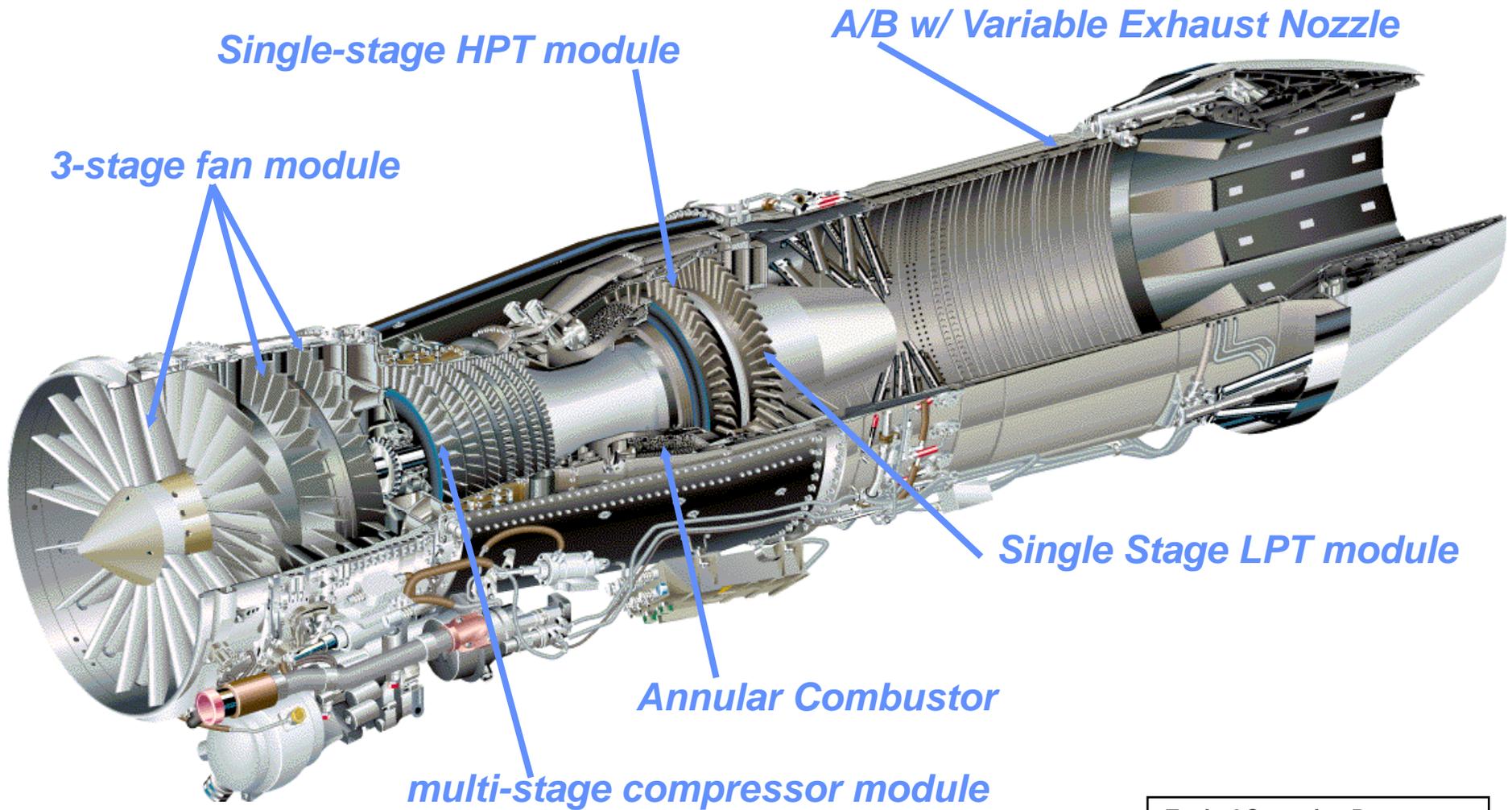
- Specific Fuel Consumption (SFC)

$$SFC = W_f / F_{net} \quad (\text{lbm/hr/lbf})$$

(lower SFC is better)



# Modern Afterburning Turbofan Engine



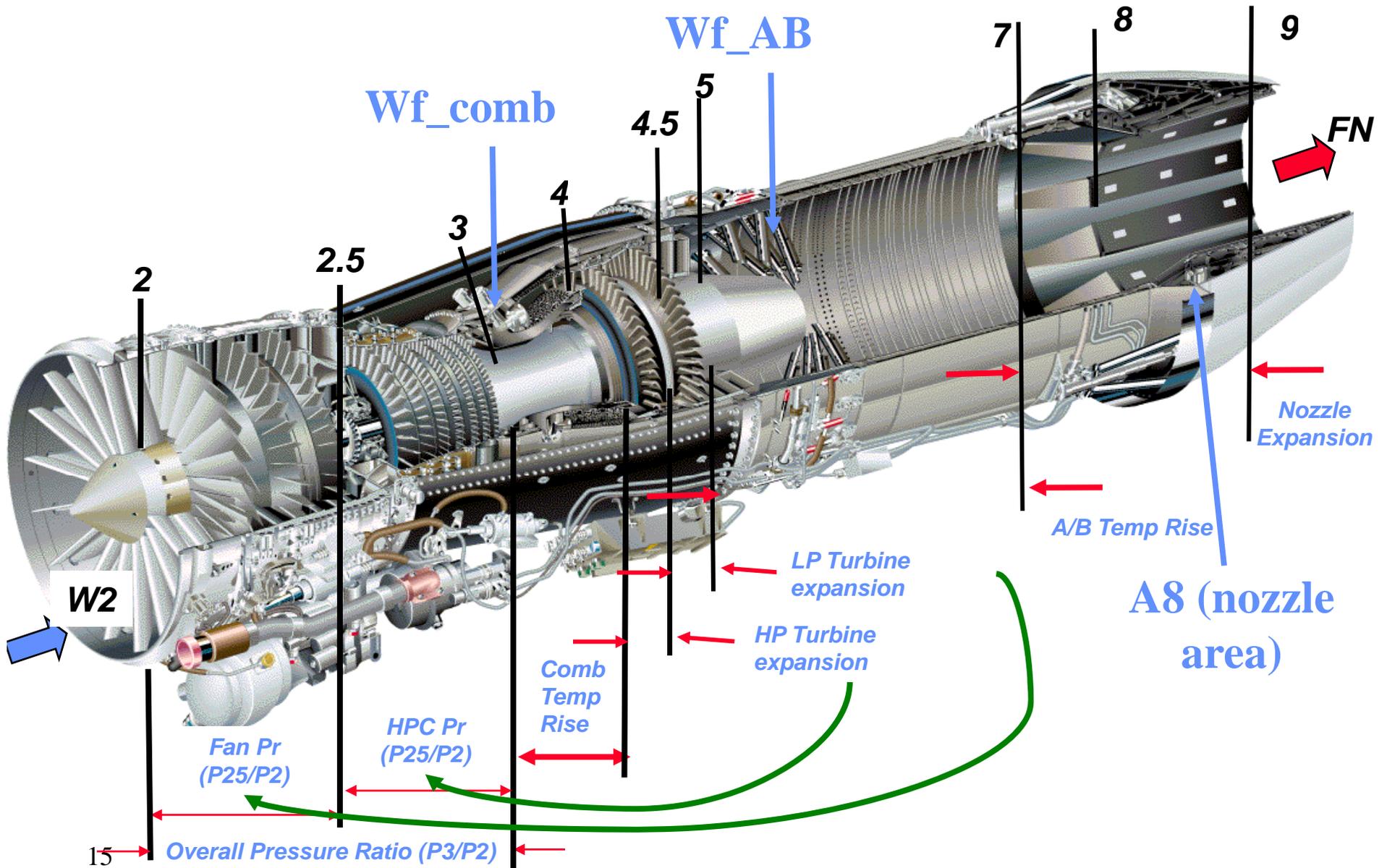
<u>Terms:</u>	
blade	rotating airfoil
vane	static airfoil
stage	rotor/stator pair
PLA	pilot's throttle

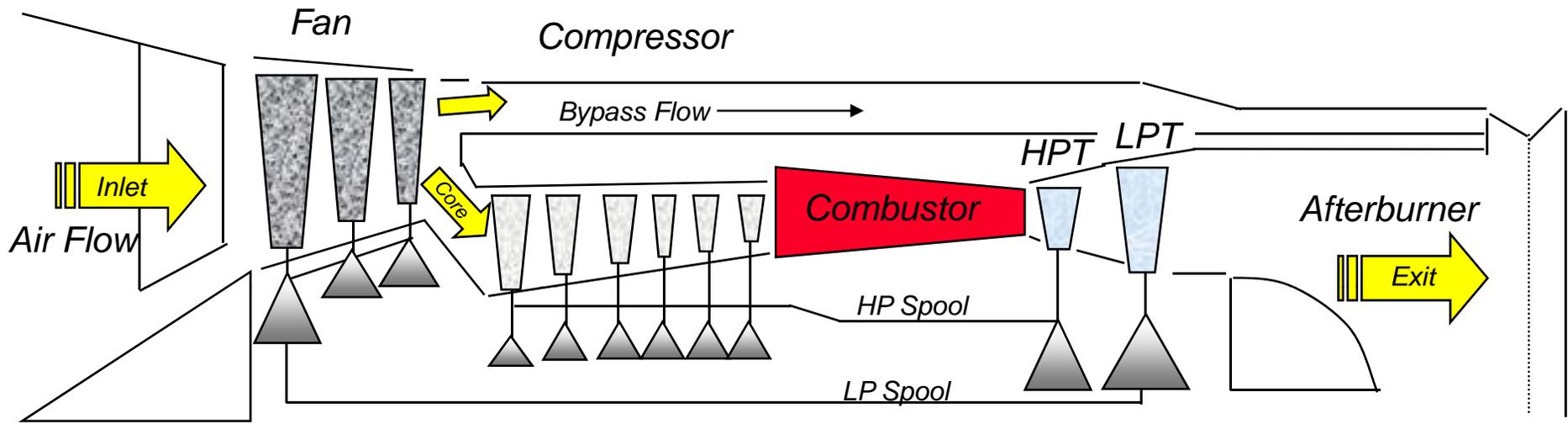
<u>Typical Operating Parameters:</u>	
OPR	25:1
BPR	0.34
ITT	2520°F
Airflow	142 lbm/sec
Thrust Class	16K-22K lbf

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# Thermodynamic Station Representation

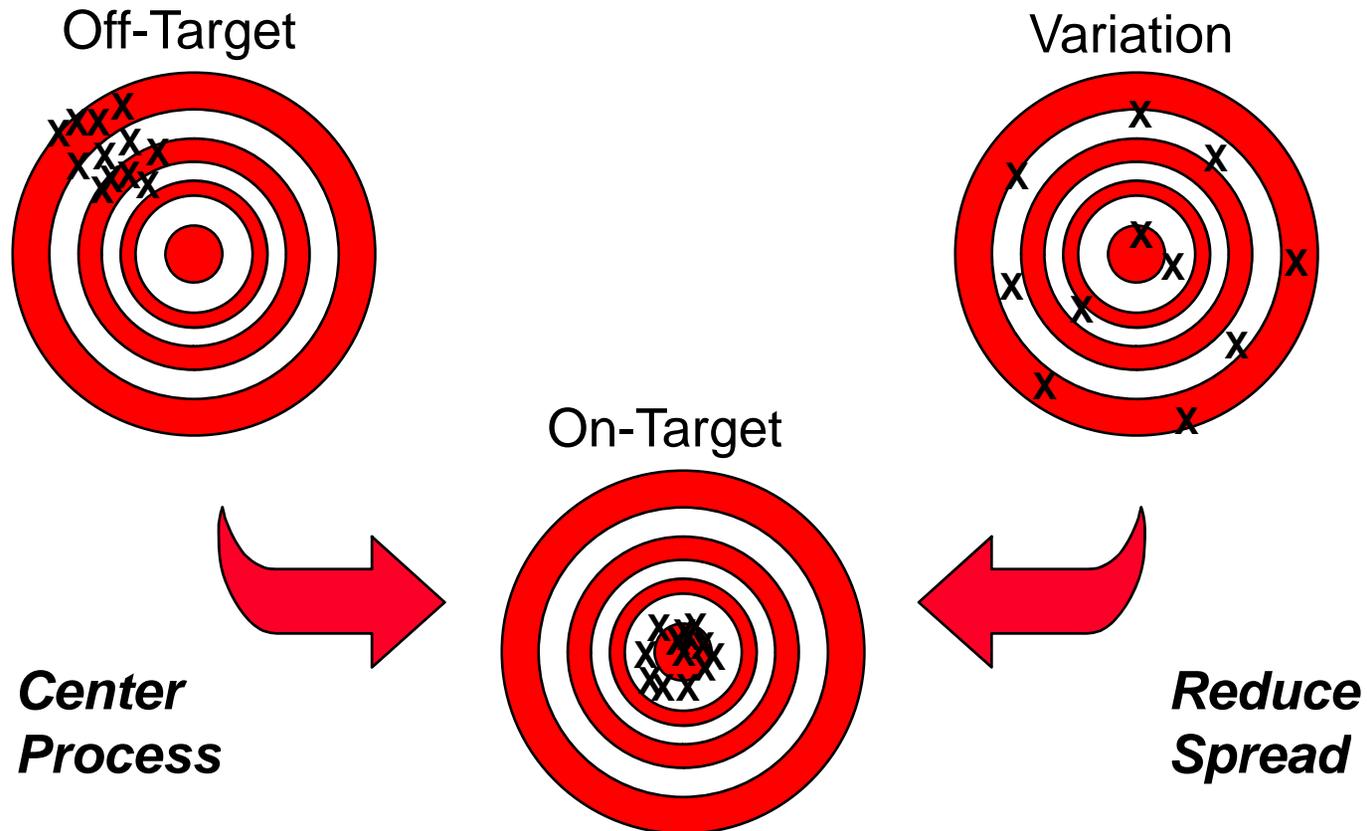
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## Augmented Turbofan Engine Cross-Section

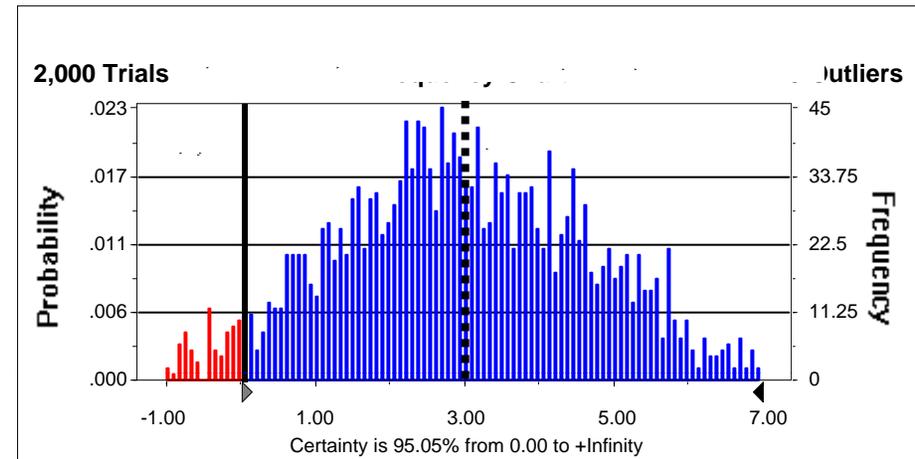
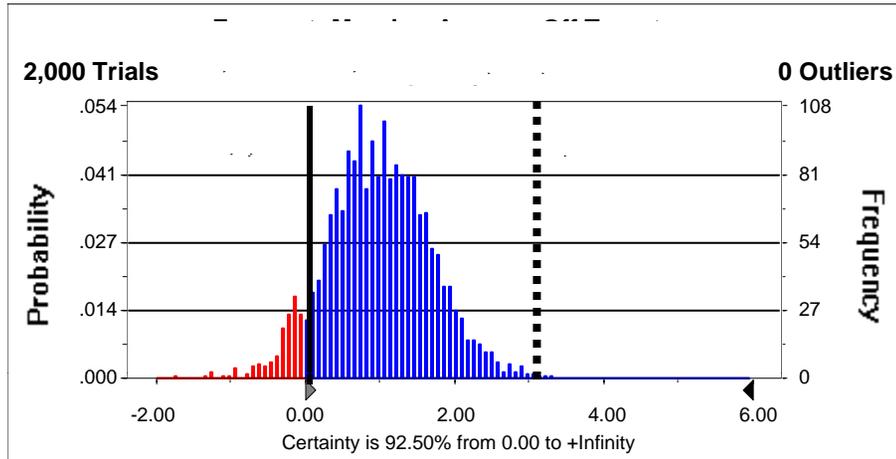
## Design Considerations- Process Centering and Variation



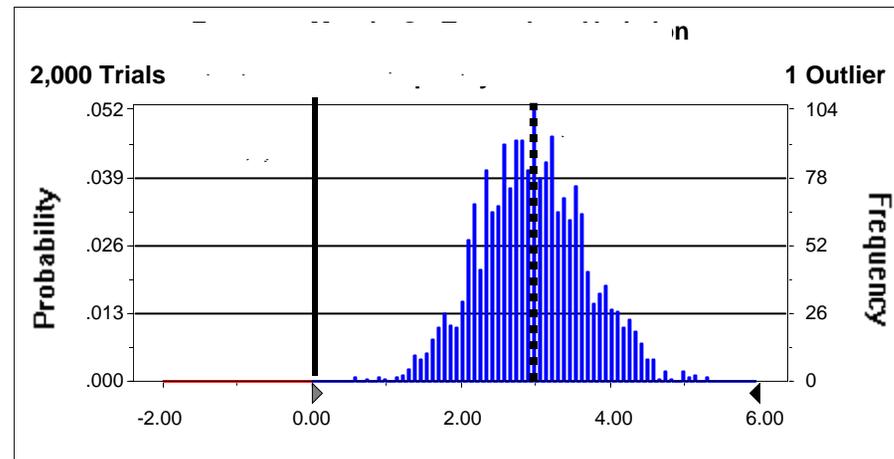
*Six Sigma Methodology Applies Statistical Analyses to Center Processes and Minimize Variation*

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## Probabilistic Design Techniques Account for Process Variation



**Center  
Process**



**Reduce  
Spread**

*Understanding and Accounting for Process Variation Assures Compliance with Design Limits*